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# pyUmbral Documentation

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pyUmbral is the reference implementation of the [Umbral](#) threshold proxy re-encryption scheme. It is open-source, built with Python, and uses [OpenSSL](#) via [Cryptography.io](#), and [libsodium](#) via [PyNaCl](#).

Using Umbral, Alice (the data owner) can *delegate decryption rights* to Bob for any ciphertext intended to her, through a re-encryption process performed by a set of semi-trusted proxies or *Ursulas*. When a threshold of these proxies participate by performing re-encryption, Bob is able to combine these independent re-encryptions and decrypt the original message using his private key.

pyUmbral is the cryptographic engine behind [nucypher](#), a proxy re-encryption network to empower privacy in decentralized systems.



# CHAPTER 1

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## Installing pyUmbral

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### 1.1 Using pip

The easiest way to install pyUmbral is using pip:

```
$ pip3 install umbral
```

### 1.2 Build from source code

pyUmbral is maintained on GitHub: <https://github.com/nucypher/pyUmbral>.

Clone the repository to download the source code.

```
$ git clone https://github.com/nucypher/pyUmbral.git
```

Once you have acquired the source code, you can...

*...embed pyUmbral modules into your own codebase...*

```
from umbral import pre, keys, config
```

*...install pyUmbral with pipenv...*

```
$ pipenv install .
```

*...or install it with python-pip...*

```
$ pip3 install .
```

## 1.3 Install dependencies

The NuCypher team uses pipenv for managing pyUmbra's dependencies. The recommended installation procedure is as follows:

```
$ sudo pip3 install pipenv  
$ pipenv install
```

Post-installation, you can activate the pyUmbra's virtual environment in your current terminal session by running `pipenv shell`.

If your installation is successful, the following command will succeed without error.

```
$ pipenv run python  
>>> import umbra
```

For more information on pipenv, The official documentation is located here: <https://docs.pipenv.org/>.

## 1.4 Development Installation

If you want to participate in developing pyUmbra, you'll probably want to run the test suite and / or build the documentation, and for that, you must install some additional development requirements.

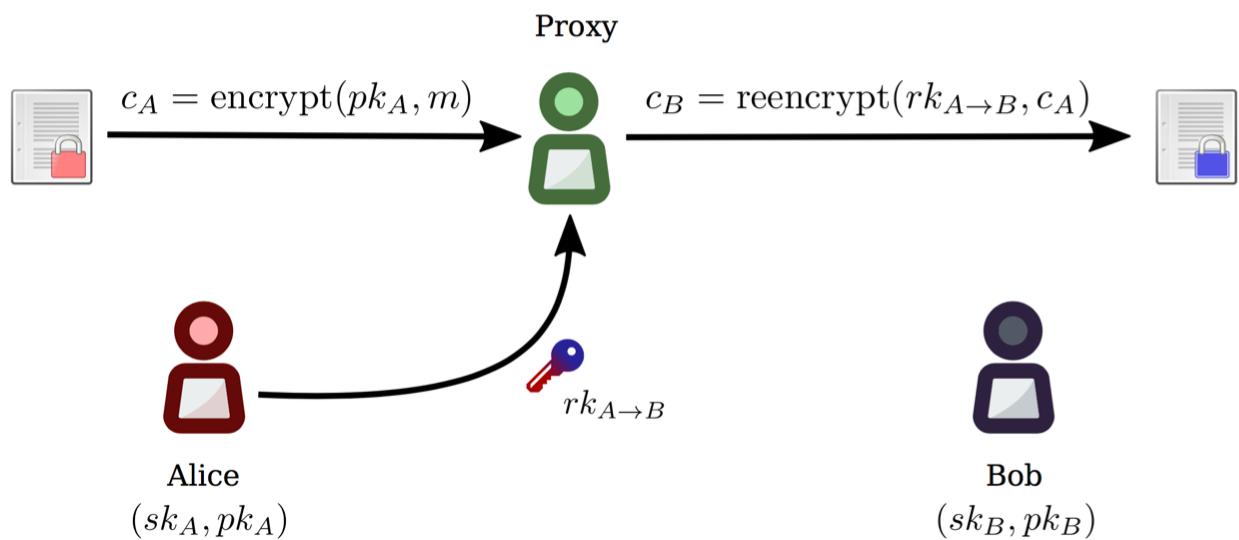
```
$ pipenv install --dev --three
```

To build the documentation locally:

```
$ pipenv run make html --directory=docs
```

# CHAPTER 2

## Using pyUmbra



## 2.1 Elliptic Curves

The matter of which curve to use is the subject of some debate. If you aren't sure, you might start here: <https://safecurves.cr.yp.to/>

A number of curves are available in the [Cryptography.io](#) library, on which pyUmbra depends. You can find them in the `cryptography.hazmat.primitives.asymmetric.ec` module.

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**Important:** Be careful when choosing a curve - the security of your application depends on it.

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We provide curve SECP256K1 as a default because it is the basis for a number of crypto-blockchain projects; we don't otherwise endorse its security. We additionally support curves SECP256R1 (also known as "NIST P-256") and SECP384R1 ("NIST P-384"), but they cannot currently be selected via the public API.

## 2.2 Encryption

### 2.2.1 Generate an Umbral key pair

First, let's generate two asymmetric key pairs for Alice: A delegating key pair and a signing key pair.

```
>>> from umbral import SecretKey, Signer

>>> alices_secret_key = SecretKey.random()
>>> alices_public_key = alices_secret_key.public_key()

>>> alices_signing_key = SecretKey.random()
>>> alices_verifying_key = alices_signing_key.public_key()
>>> alices_signer = Signer(alices_signing_key)
```

### 2.2.2 Encrypt with a public key

Now let's encrypt data with Alice's public key. Invocation of `umbral.encrypt()` returns both a capsule and a ciphertext. Note that anyone with Alice's public key can perform this operation.

```
>>> from umbral import encrypt
>>> plaintext = b'Proxy Re-encryption is cool!'
>>> capsule, ciphertext = encrypt(alices_public_key, plaintext)
```

### 2.2.3 Decrypt with a private key

Since data was encrypted with Alice's public key, Alice can open the capsule and decrypt the ciphertext with her private key.

```
>>> from umbral import decrypt_original
>>> cleartext = decrypt_original(alices_secret_key, capsule, ciphertext)
```

## 2.3 Threshold Re-Encryption

### 2.3.1 Bob Exists

```
>>> bobs_secret_key = SecretKey.random()
>>> bobs_public_key = bobs_secret_key.public_key()
```

### 2.3.2 Alice grants access to Bob by generating kfrags

When Alice wants to grant Bob access to view her encrypted data, she creates *re-encryption key fragments*, or "kfrags", which are next sent to N proxies or *Ursulas*.

Alice must specify `shares` (the total number of kfrags), and a `threshold` (the minimum number of kfrags needed to activate a capsule). In the following example, Alice creates 20 kfrags, but Bob needs to get only 10 re-encryptions to activate the capsule.

```
>>> from umbral import generate_kfrags
>>> kfrags = generate_kfrags(delegating_sk=alices_secret_key,
...                             receiving_pk=bobs_public_key,
...                             signer=alices_signer,
...                             threshold=10,
...                             shares=20)
```

### 2.3.3 Bob receives a capsule

Next, let's generate a key pair for Bob, and pretend to send him the capsule through a side channel like S3, IPFS, Google Cloud, Sneakernet, etc.

```
# Bob receives the capsule through a side-channel: IPFS, Sneakernet, etc.
capsule = <fetch the capsule through a side-channel>
```

### 2.3.4 Bob fails to open the capsule

If Bob attempts to open a capsule that was not encrypted for his public key, or re-encrypted for him by Ursula, he will not be able to open it.

```
>>> fail = decrypt_original(delegating_sk=bobs_secret_key,
...                           capsule=capsule,
...                           ciphertext=ciphertext)
Traceback (most recent call last):
...
ValueError
```

### 2.3.5 Ursulas perform re-encryption

Bob asks several Ursulas to re-encrypt the capsule so he can open it. Each Ursula performs re-encryption on the capsule using the `kfrag` provided by Alice, obtaining this way a “capsule fragment”, or `cfrag`. Let's mock a network or transport layer by sampling `threshold` random kfrags, one for each required Ursula.

Bob collects the resulting `cfrags` from several Ursulas. Bob must gather at least `threshold` `cfrags` in order to open the capsule.

```
>>> import random
>>> kfrags = random.sample(kfrags,    # All kfrags from above
...                           10)      # M - Threshold

>>> from umbral import reencrypt
>>> cfrags = list()                      # Bob's cfrag collection
>>> for kfrag in kfrags:
...     cfrag = reencrypt(capsule=capsule, kfrag=kfrag)
...     cfrags.append(cfrag)                 # Bob collects a cfrag
```

## 2.4 Decryption

### 2.4.1 Bob checks the capsule fragments

If Bob received the capsule fragments in serialized form, he can verify that they are valid and really originate from Alice, using Alice's public keys.

```
>>> from umbral import CapsuleFrag
>>> suspicious_cfrags = [CapsuleFrag.from_bytes(bytes(cfrag)) for cfrag in cfrags]
>>> cfrags = [cfrag.verify(capsule,
...                 verifying_pk=alices_verifying_key,
...                 delegating_pk=alices_public_key,
...                 receiving_pk=bobs_public_key,
...                 )
... for cfrag in suspicious_cfrags]
```

### 2.4.2 Bob opens the capsule

Finally, Bob decrypts the re-encrypted ciphertext using his key.

```
>>> from umbral import decrypt_reencrypted
>>> cleartext = decrypt_reencrypted(receiving_sk=bobs_secret_key,
...                                 delegating_pk=alices_public_key,
...                                 capsule=capsule,
...                                 verified_cfrags=cfrags,
...                                 ciphertext=ciphertext)
```

# CHAPTER 3

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## Public API

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### 3.1 Keys

```
class umbral.SecretKey
Bases: umbral.serializable.SerializableSecret, umbral.serializable.
Deserializable

Umbral secret (private) key.

public_key() → umbral.keys.PublicKey
    Returns the associated public key.

classmethod random() → umbral.keys.SecretKey
    Generates a random secret key and returns it.

classmethod serialized_size()
    Returns the size in bytes of the serialized representation of this object (obtained with bytes() or
    to_secret_bytes()).

to_secret_bytes() → bytes
    Serializes the object into bytes. This bytestring is secret, handle with care!

class umbral.PublicKey
Bases: umbral.serializable.Serializable, umbral.serializable.Deserializable

Umbral public key.

Created using SecretKey.public_key().

__eq__(other)
    Return self==value.

__hash__() → int
    Return hash(self).

classmethod serialized_size()
    Returns the size in bytes of the serialized representation of this object (obtained with bytes() or
    to_secret_bytes()).
```

```
class umbral.SecretKeyFactory
Bases: umbral.serializable.SerializableSecret, umbral.serializable.Deserializable
```

This class handles keyring material for Umbral, by allowing deterministic derivation of `SecretKey` objects based on labels.

Don't use this key material directly as a key.

```
classmethod from_secure_randomness(seed: bytes) → umbral.keys.SecretKeyFactory
Creates a secret key factory using the given random bytes (of size seed_size()).
```

**Warning:** Make sure the given seed has been obtained from a cryptographically secure source of randomness!

```
make_factory(label: bytes) → umbral.keys.SecretKeyFactory
Creates a SecretKeyFactory deterministically from the given label.
```

```
make_key(label: bytes) → umbral.keys.SecretKey
Creates a SecretKey deterministically from the given label.
```

```
classmethod random() → umbral.keys.SecretKeyFactory
Creates a random factory.
```

```
classmethod seed_size()
Returns the seed size required by from_secure_randomness().
```

```
classmethod serialized_size()
Returns the size in bytes of the serialized representation of this object (obtained with bytes() or to_secret_bytes()).
```

```
to_secret_bytes() → bytes
Serializes the object into bytes. This bytestring is secret, handle with care!
```

```
class umbral.Signer(secret_key: umbral.keys.SecretKey)
```

An object possessing the capability to create signatures. For safety reasons serialization is prohibited.

```
sign(message: bytes) → umbral.signing.Signature
Hashes and signs the message.
```

```
verifying_key() → umbral.keys.PublicKey
Returns the public verification key corresponding to the secret key used for signing.
```

```
class umbral.Signature
```

Bases: `umbral.serializable.Serializable`, `umbral.serializable.Deserializable`

Wrapper for ECDSA signatures.

```
__eq__(other)
Return self==value.
```

```
__hash__() → int
Return hash(self).
```

```
classmethod serialized_size()
```

Returns the size in bytes of the serialized representation of this object (obtained with bytes() or to\_secret\_bytes()).

```
verify(verifying_pk: umbral.keys.PublicKey, message: bytes) → bool
```

Returns True if the message was signed by someone possessing the secret counterpart to `verifying_pk`.

## 3.2 Intermediate objects

```
class umbral.Capsule
    Bases: umbral.serializable.Serializable, umbral.serializable.Deserializable

    Encapsulated symmetric key.

    __eq__(other)
        Return self==value.

    __hash__()
        Return hash(self).

class umbral.KeyFrag
    Bases: umbral.serializable.Serializable, umbral.serializable.Deserializable

    A signed fragment of the delegating key.

    __eq__(other)
        Return self==value.

    __hash__()
        Return hash(self).

verify(verifying_pk: umbral.keys.PublicKey, delegating_pk: Optional[umbral.keys.PublicKey]
        = None, receiving_pk: Optional[umbral.keys.PublicKey] = None) → umbral.key_frag.VerifiedKeyFrag
    Verifies the validity of this fragment.

    If the delegating and/or receiving key were not signed in generate_k frags(), but are given to this
    function, they are ignored.

class umbral.VerifiedKeyFrag
    Bases: umbral.serializable.Serializable

    Verified kfrag, good for reencryption. Can be cast to bytes, but cannot be deserialized from bytes directly. It
    can only be obtained from KeyFrag.verify().

    __eq__(other)
        Return self==value.

    __hash__()
        Return hash(self).

    classmethod from_verified_bytes(data) → umbral.key_frag.VerifiedKeyFrag
        Restores a verified keyfrag directly from serialized bytes, skipping KeyFrag.verify() call.

        Intended for internal storage; make sure that the bytes come from a trusted source.

    classmethod serialized_size()
        Returns the size in bytes of the serialized representation of this object (obtained with bytes() or
        to_secret_bytes()).

class umbral.CapsuleFrag
    Bases: umbral.serializable.Serializable, umbral.serializable.Deserializable

    Re-encrypted fragment of Capsule.

    __eq__(other)
        Return self==value.

    __hash__()
        Return hash(self).
```

```
classmethod serialized_size()
    Returns the size in bytes of the serialized representation of this object (obtained with bytes() or
    to_secret_bytes()).

verify(capsule: umbral.capsule.Capsule, verifying_pk: umbral.keys.PublicKey, delegat-
ing_pk: umbral.keys.PublicKey, receiving_pk: umbral.keys.PublicKey) → um-
bral.capsule_frag.VerifiedCapsuleFrag
    Verifies the validity of this fragment.

class umbral.VerifiedCapsuleFrag
    Bases: umbral.serializable.Serializable

    Verified capsule frag, good for decryption. Can be cast to bytes, but cannot be deserialized from bytes directly.
    It can only be obtained from CapsuleFrag.verify().

    __eq__(other)
        Return self==value.

    __hash__()
        Return hash(self).

classmethod from_verified_bytes(data) → umbral.capsule_frag.VerifiedCapsuleFrag
    Restores a verified capsule frag directly from serialized bytes, skipping CapsuleFrag.verify() call.

    Intended for internal storage; make sure that the bytes come from a trusted source.

classmethod serialized_size()
    Returns the size in bytes of the serialized representation of this object (obtained with bytes() or
    to_secret_bytes()).
```

### 3.3 Encryption, re-encryption and decryption

```
umbral.encrypt(delegating_pk: umbral.keys.PublicKey, plaintext: bytes) → Tu-
    ple[umbral.capsule.Capsule, bytes]
    Generates and encapsulates a symmetric key and uses it to encrypt the given plaintext.

    Returns the KEM Capsule and the ciphertext.

umbral.decrypt_original(delegating_sk: umbral.keys.SecretKey, capsule: umbral.capsule.Capsule,
    ciphertext: bytes) → bytes
    Opens the capsule using the delegator's key used for encryption and gets what's inside. We hope that's a
    symmetric key, which we use to decrypt the ciphertext and return the resulting cleartext.

umbral.generate_k frags(delegating_sk: umbral.keys.SecretKey, receiving_pk: um-
    bral.keys.PublicKey, signer: umbral.signing.Signer, threshold: int, shares:
    int, sign_delegating_key: bool = True, sign_receiving_key: bool = True) →
    List[umbral.key_fraq.VerifiedKeyFrag]
    Generates shares key fragments to pass to proxies for re-encryption. At least threshold of them will be
    needed for decryption. If sign_delegating_key or sign_receiving_key are True, the corresponding
    keys will have to be provided to KeyFrag.verify().

umbral.reencrypt(capsule: umbral.capsule.Capsule, kfrag: umbral.key_fraq.VerifiedKeyFrag) → um-
    bral.capsule_frag.VerifiedCapsuleFrag
    Creates a capsule fragment using the given key fragment. Capsule fragments can later be used to decrypt the
    ciphertext.

umbral.decrypt_reencrypted(receiving_sk: umbral.keys.SecretKey, delegating_pk: um-
    bral.keys.PublicKey, capsule: umbral.capsule.Capsule, veri-
    fied_cfrags: Sequence[umbral.capsule_frag.VerifiedCapsuleFrag],
    ciphertext: bytes) → bytes
```

Decrypts the ciphertext using the original capsule and the reencrypted capsule fragments.

## 3.4 Utilities

**class** umbral.VerificationError

Bases: Exception

Integrity of the data cannot be verified, see the message for details.

**class** umbral.serializable.HasSerializedSize

A base serialization mixin, denoting a type with a constant-size serialized representation.

**classmethod** serialized\_size() → int

Returns the size in bytes of the serialized representation of this object (obtained with bytes() or to\_secret\_bytes()).

**class** umbral.serializable.Serializable

Bases: *umbral.serializable.HasSerializedSize*

A mixin for composable serialization.

**\_\_bytes\_\_()**

Serializes the object into bytes.

**class** umbral.serializable.SerializableSecret

Bases: *umbral.serializable.HasSerializedSize*

A mixin for composable serialization of objects containing secret data.

**to\_secret\_bytes()**

Serializes the object into bytes. This bytestring is secret, handle with care!

**class** umbral.serializable.Deserializable

Bases: *umbral.serializable.HasSerializedSize*

A mixin for composable deserialization.

**classmethod** from\_bytes(data: bytes) → Self

Restores the object from serialized bytes.



# CHAPTER 4

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## Academic Whitepaper

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The Umbral scheme academic whitepaper and cryptographic specifications are available on GitHub.

“Umbral: A Threshold Proxy Re-Encryption Scheme” by David Nuñez. <https://github.com/nucypher/umbral-doc/blob/master/umbral-doc.pdf>



# CHAPTER 5

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## Support & Contribute

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- Issue Tracker: <https://github.com/nucypher/pyUmbral/issues>
- Source Code: <https://github.com/nucypher/pyUmbral>



# CHAPTER 6

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## Security

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If you identify vulnerabilities with `_any_ nucypher` code, please email [security@nucypher.com](mailto:security@nucypher.com) with relevant information to your findings. We will work with researchers to coordinate vulnerability disclosure between our partners and users to ensure successful mitigation of vulnerabilities.

Throughout the reporting process, we expect researchers to honor an embargo period that may vary depending on the severity of the disclosure. This ensures that we have the opportunity to fix any issues, identify further issues (if any), and inform our users.

Sometimes vulnerabilities are of a more sensitive nature and require extra precautions. We are happy to work together to use a more secure medium, such as Signal. Email [security@nucypher.com](mailto:security@nucypher.com) and we will coordinate a communication channel that we're both comfortable with.



# CHAPTER 7

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